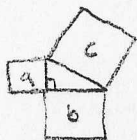


Pythagorean Theorem Defined

① If you have a right triangle



② And you make a square on each side



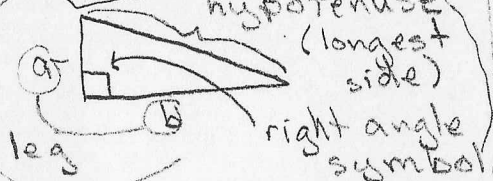
③ then the biggest square has the same area as the two smaller squares put together

$$a^2 + b^2 = c^2$$

$$a^2 + b^2 = c^2$$

Vocabulary

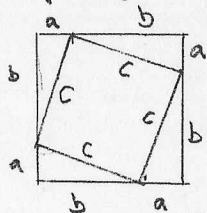
RIGHT TRIANGLE



Pythagorean Theorem

Proof

using known facts to prove something in steps



① Area of large square is:

$$A = (a+b)(a+b)$$

② Areas of smaller pieces:

$$\text{Small } \square A = c^2$$

$$\text{triangles } \Delta A = \frac{1}{2}ab$$

$$\text{all 4 } \Delta s \quad A = 4\left(\frac{1}{2}ab\right)$$

Total area of parts = $2ab$

$$A = c^2 + 2ab$$

Conclusion

Both areas must be equal

$$(a+b)(a+b) = c^2 + 2ab$$

$$a^2 + 2ab + b^2 = c^2 + 2ab$$

$$a^2 + b^2 = c^2$$

DONE!

Converse Proof

a proof that starts with the conclusion

Given: ΔABC with $a^2 + b^2 = c^2$
 prove ΔABC is a Δ
 6cm 10cm 8cm

$$6^2 + 8^2 = 10^2$$

$$36 + 64 = 100$$

$$100 = 100 \checkmark$$

what would make an acute Δ ?

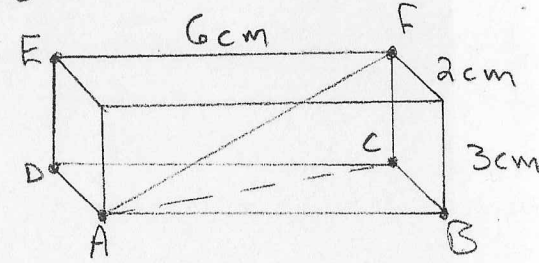
$$\text{If } c^2 < a^2 + b^2$$

Obtuse Δ ?

$$\text{If } c^2 > a^2 + b^2$$

corollary to the converse

Finding an unknown length in 2 Dimensional & 3D Figures



Find length of AF using Pythagorean Theorem

① ΔABC

$$AC^2 = 6^2 + 2^2$$

$$AC^2 = 36 + 4$$

$$AC^2 = 40$$

$$AC = \sqrt{40}$$

② ΔACF

$$AF^2 = AC^2 + CF^2$$

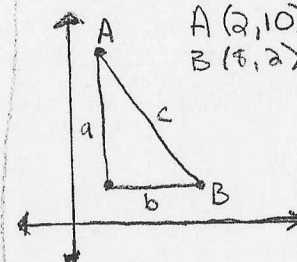
$$AF^2 = 40 + 3^2$$

$$AF^2 = 49$$

$$AF = \sqrt{49}$$

$$AF = 7 \text{ cm}$$

Using the coordinate system



A(2,10)
B(8,2)

$$c^2 = a^2 + b^2$$

$$c^2 = 8^2 + 6^2$$

$$c^2 = 64 + 36$$

$$c^2 = 100$$

$$c = 10$$

Mathematical Standards and Practices

• We will attend to precision when using terminology to refer to geometric figures.

• We will construct viable arguments and critique the reasoning of others when explaining a proof of the Pythagorean theorem and its converse.

We know...

Inquiry
Pythagorean Theorem

We want to know...

UNIT PLANNING TOOL

Unit 8th: Geometry

CCSSM: 8.G.B.6

Math Practices being emphasized:

- #3 Construct viable arguments and critique the reasoning of others
- #6 Attend to precision

- 8.G.B.6 Explain a proof of Pythagorean Theorem and its Converse
- 8.G.B.7 Apply Pythagorean Theorem to determine unknown side lengths in right triangles in real and mathematical problems with 2D & 3D figures

- 8.G.B.8 Apply Pythagorean Theorem to find distances between points on coordinate systems

Essential Questions

How can Pythagorean Theorem be used to solve problems?
How do I know that I have a convincing argument to informally prove PT?

Pre

Pre and Post Assessments

Post

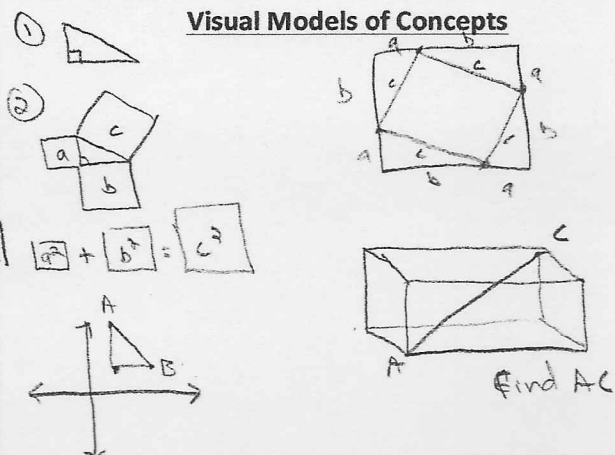
Teacher Made
see attached

- unit assessment
- Performance Task

Key Concepts

- Coordinates can be used to measure distances
- Right triangles have a special relationship among the side lengths which can be represented by a model and a formula
- Recognizing Pythagorean Theorem Triples can increase efficiency with problems involving PT

Visual Models of Concepts



Algorithms/Diagrams

$$a^2 + b^2 = c^2$$

if $c^2 < a^2 + b^2$ then acute Δ

if $c^2 > a^2 + b^2$ then obtuse Δ

$$A_{\square} = (a+b)(a+b)$$

$$A_{\Delta} = \frac{1}{2}(ab)$$

$$\times 4 = 4\left(\frac{1}{2}\right)ab$$

$$= 2ab$$

$$A_{\square} = c^2$$

$$(a+b)(a+b) = c^2 + 2ab$$

Connections (Real World Applications)

- Be able to find an unknown length
- Be able to find a difficult length to measure
- Carpentry
- Engineers
- Architects
- Construction
- Sculpture
- Art

Explain

Language Functions/Structures

If you have _____ then you can determine _____.

Compare

This area must be equal to that area because _____.

Altitude of triangle

Base (of a polygon)

Coordinate Plane

Converse of Pythagorean Theorem

Cubic Root

Hypotenuse

Vocabulary

Leg of a triangle

Perfect Squares

Perfect Cubes

Pythagorean Theorem

Pythagorean Triples

Square Root

Right Triangle

Literature

What's your Angle,
Pythagoras?
by Julie Ellis

Animation

Brainpop
- Pythagorean
Theorem

Focus and Motivation

Tools of Trade

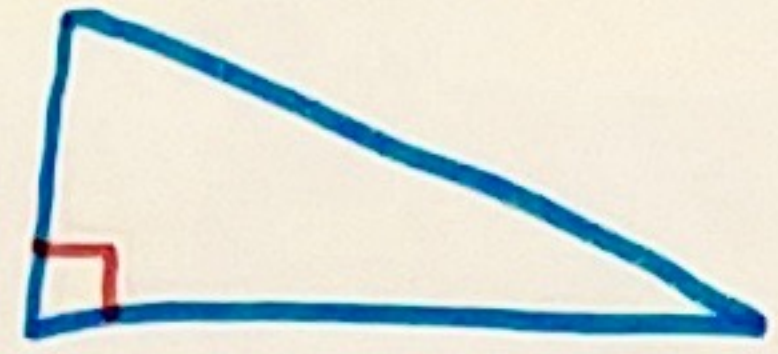
- right angle
- framing square
- Sliding T-bevel
- Level

Art

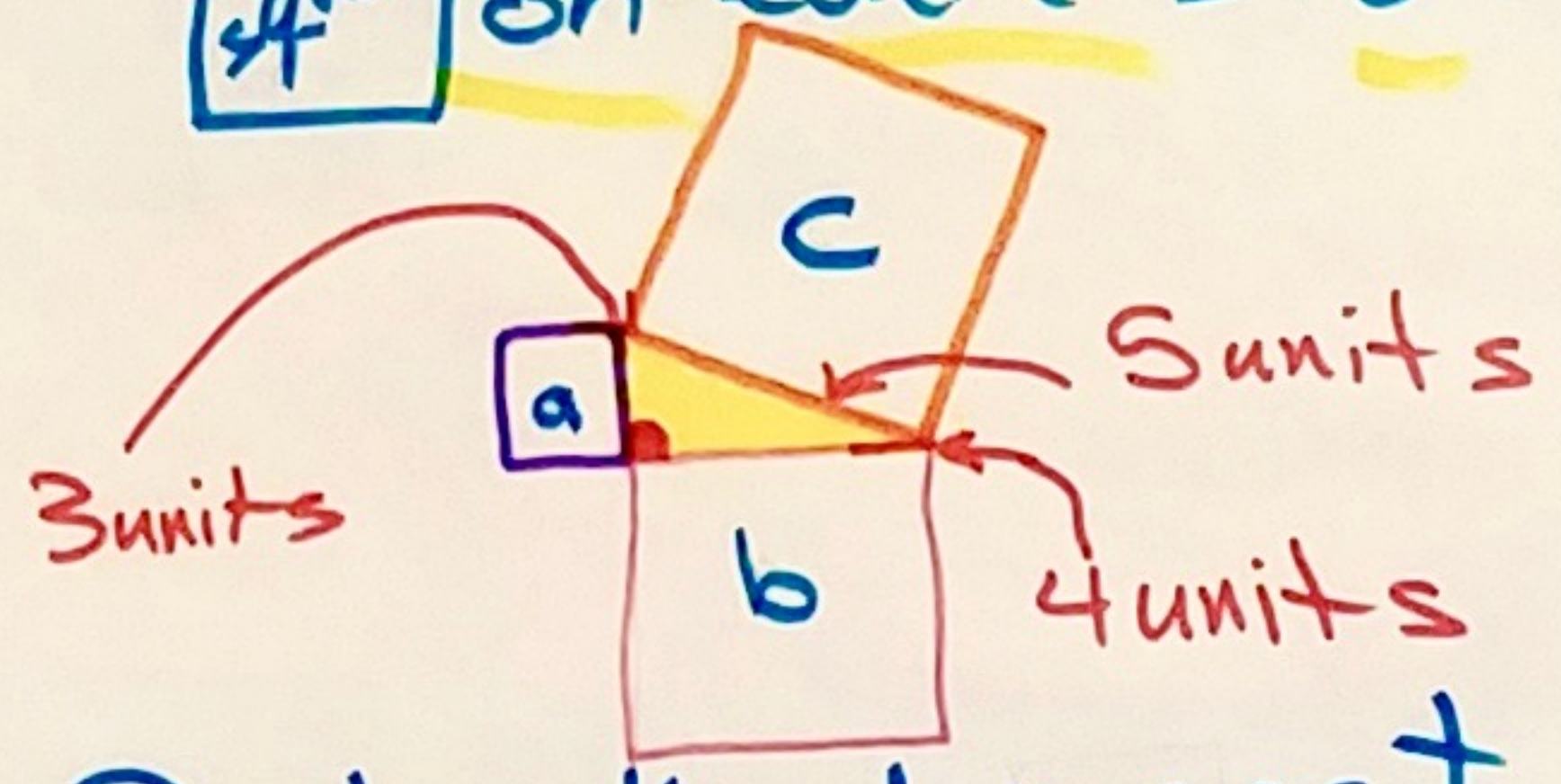
Pythagorean Spiral
Pythagorean Tree

Pythagorean Theorem Defined

① If you have a right triangle



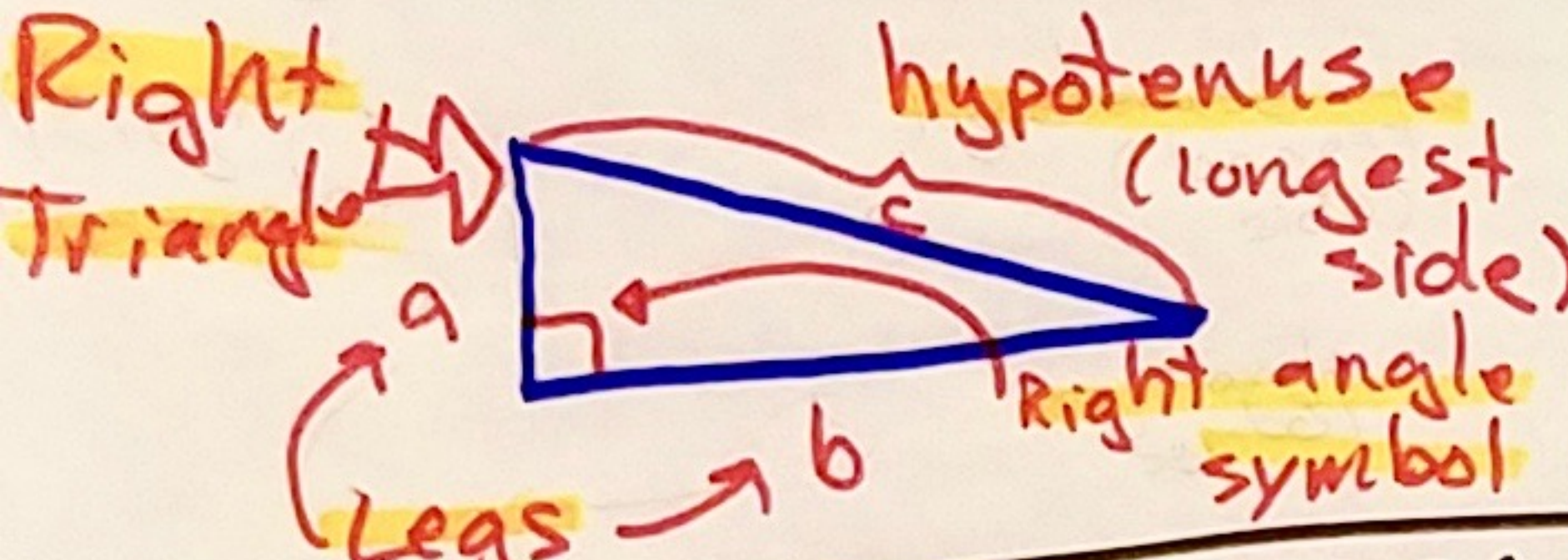
② And you make a square on each side



③ then the biggest has the same area as the two smaller put together

$$a^2 + b^2 = c^2$$

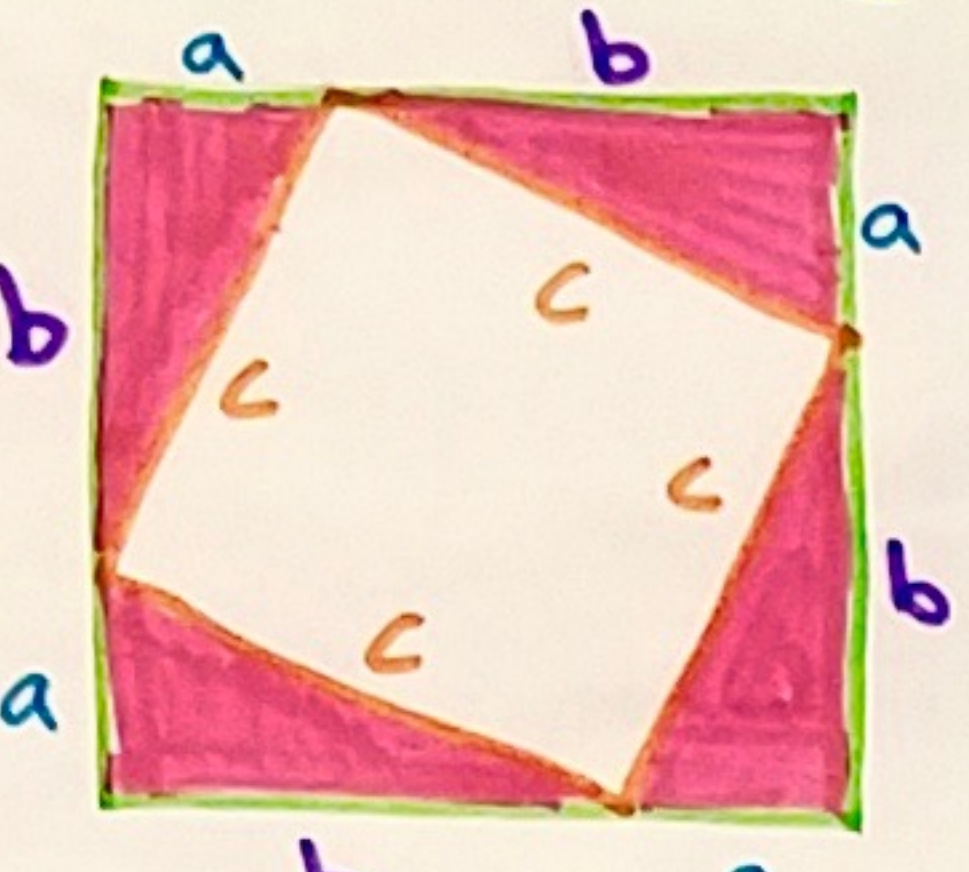
Vocabulary



PYTHAGOREAN THEOREM

Proof

using known facts to prove something in steps



① Area of large square is:

$$A_{\square} = (a+b)(a+b)$$

② Area of smaller pieces:

$$\begin{aligned} \text{Small } \square A_{\square} &= c^2 \\ \text{Triangles } A_{\Delta} &= \frac{1}{2}(ab) \\ \text{All 4 } A_{\Delta} &= 4(\frac{1}{2}ab) \\ A_{\Delta} &= 2ab \end{aligned}$$

Total Area of parts:

$$A_{\text{Total}} = c^2 + 2ab$$

Conclusion

$$\begin{aligned} \text{Both areas must be EQUAL} \\ (a+b)(a+b) &= c^2 + 2ab \\ a^2 + 2ab + b^2 &= c^2 + 2ab \\ \boxed{a^2 + b^2 = c^2} & \text{ DONE!} \end{aligned}$$

Converse Proof

a proof that starts with the conclusion

GIVEN: $\triangle ABC$ with $a^2 + b^2 = c^2$

Prove $\triangle ABC$ is a right triangle

$$\begin{aligned} \text{Sides } 6\text{ cm } 8\text{ cm } 10\text{ cm} \\ 6^2 + 8^2 &= 10^2 \\ 36 + 64 &= 100 \\ 100 &= 100 \checkmark \end{aligned}$$

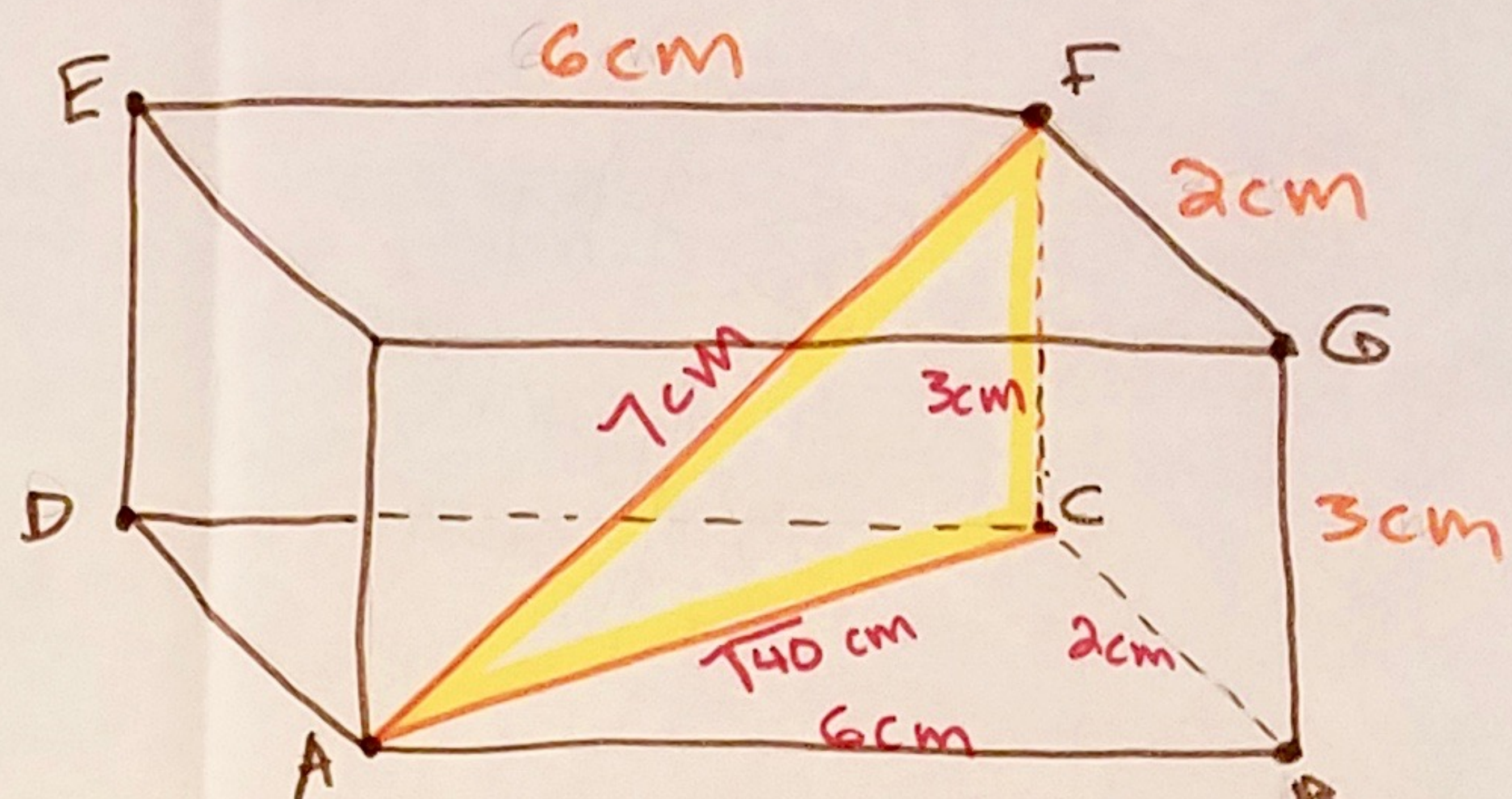
What would make an acute $\triangle$?

$$\text{If } c^2 < a^2 + b^2$$

What would make an obtuse $\triangle$?

$$\text{If } c^2 > a^2 + b^2$$

Finding an unknown length in 2D and 3D Figures



Find length AF using Pythagorean Theorem

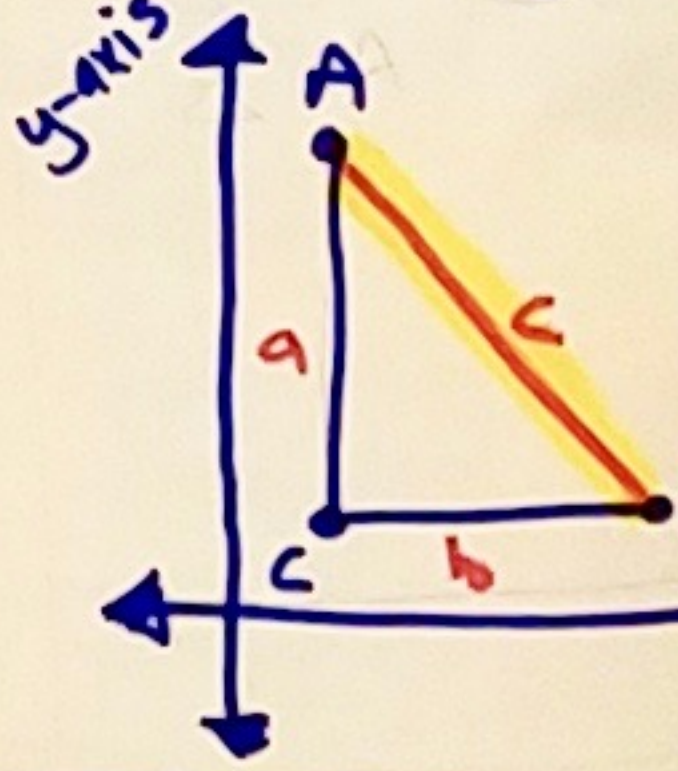
① $\triangle ABC$

$$\begin{aligned} AC^2 &= 6^2 + 2^2 \\ AC^2 &= 36 + 4 \\ AC^2 &= 40 \\ AC &= \sqrt{40} \end{aligned}$$

② $\triangle ACF$

$$\begin{aligned} AF^2 &= AC^2 + CF^2 \\ AF^2 &= 40 + 3^2 \\ AF^2 &= 49 \\ AF &= \sqrt{49} \\ \boxed{AF = 7\text{ cm}} \end{aligned}$$

Using the Coordinate System



$$\begin{aligned} A(2, 10) \quad c^2 &= a^2 + b^2 \\ B(8, 2) \quad c^2 &= 8^2 + 6^2 \\ \text{Find length } c \text{ (hypotenuse)} \quad c^2 &= 64 + 36 \\ c^2 &= 100 \\ c &= 10 \end{aligned}$$

Mathematical Standards & Practices

- We will attend to precision when using terminology to refer to geometric figures.
- We will construct viable arguments and critique the reasoning of others when explaining a proof of the Pythagorean Theorem and its converse.

We know...

It has to do with angles.

It has to do with right angles.

It has to do with $\triangle$. The legs are mostly with right angles (the sides).

? Inquiry?

Pythagorean Theorem

We want to know...

What is the Pythagorean theorem?

Why do we need it in our everyday life?

How to use it? We can find an unknown measurement that is hard to physically measure.