

Multiplication

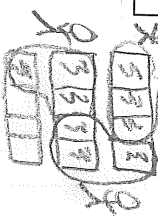
$$3 \times 4 = 12$$

3 + 3 + 3 + 3
 multiplication = repeated addition

Whole number by a fraction

3 students each ate $\frac{3}{4}$ of a candy bar. How many candy bars did they eat?

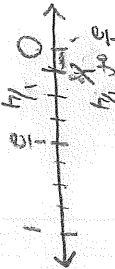
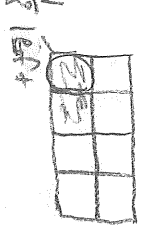
$$3 \times \frac{3}{4} = 2\frac{1}{4}$$



Fraction by a fraction

I have $\frac{1}{4}$ of a lasagna left. If we eat $\frac{1}{2}$ of it for dinner. How much do we have for lunch tomorrow?

$$\frac{1}{2} \times \frac{1}{4} = \frac{1}{8}$$



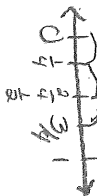
Mathematical Standards and Practices

- 1) We will use modeling to explain our mathematical thinking when multiplying and dividing fractions.
- 2) We will solve real-world problems involving multiplication and division of fractions by making sense of problems and persevering in solving them.

Multiplying and Dividing Fractions

Types of Fractions

Proper fraction: $\frac{3}{4}$
 Parts \rightarrow 3 numerator
 Whole \rightarrow 4 denominator



Improper fraction: $\frac{5}{4}$
 Mixed number: $1\frac{1}{4}$

$$\frac{5}{4} = 1\frac{1}{4}$$

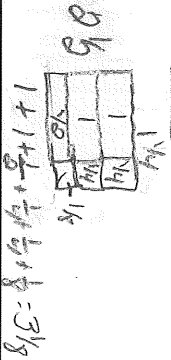


Mixed number by a mixed number

Juan bought $2\frac{1}{2}$ pounds of grapes. He also bought bananas that were $1\frac{1}{2}$ times the weight of the grapes. How much did the bananas weigh?

$$2\frac{1}{2} \times 1\frac{1}{2} = 3\frac{3}{4}$$

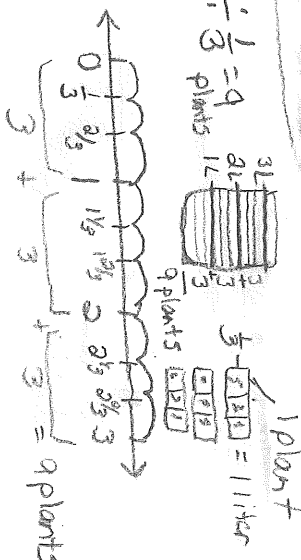
Partial products = 1 unit



- 1) $2 \times 1 = 2$
 - 2) $2 \times \frac{1}{2} = 1$
 - 3) $\frac{1}{2} \times 1 = \frac{1}{2}$
 - 4) $\frac{1}{2} \times \frac{1}{2} = \frac{1}{4}$
- $2 + 1 + \frac{1}{2} + \frac{1}{4} = 3\frac{3}{4}$

The container holds 3 liters of water. Each plant needs $\frac{1}{3}$ liter. How many plants can we water?

$$3 \div \frac{1}{3} = 9$$



Unit fraction by a whole number

$\frac{1}{2}$ of a bag of marbles is shared by 3 people. What fraction of the bag of marbles will each person get?

$$\frac{1}{2} \div 3 = \frac{1}{6}$$



Partial numbers

$\frac{1}{2} = .5 = 50\%$
 Fractions, decimals, percents

Division

$$6 \div 2 = 3$$

Whole number by a unit fraction

Inquiry Chart

What we know about _____? What we want to learn about _____?

Multiplying and dividing fractions

UNIT PLANNING TOOL

Planning Focus: Fractions: Multiplication and Division

Grade Level: 5th

CCSSM: MGSE5.NF.4 Apply and extend previous understandings of multiplication to multiply a fraction or whole number by a fraction.

MGSE5.NF.6 Solve real world problems involving multiplication of fractions and mixed numbers, e.g., by using visual fraction models or equations to represent the problem.

MGSE5.NF.7 Apply and extend previous understandings of division to divide unit fractions by whole numbers and whole numbers by unit fractions (includes solving real-world problems).

Mathematical Practices being emphasized:

3. Construct viable arguments and critique the reasoning of others.
4. Model with mathematics.

Essential Questions

How can a fraction model help us make sense of a problem?

How can real-world situations help us understand what it means to multiply and divide fractions?

Key Concepts

- Benchmark fractions
- Plotting fractions on a number line
- Use visual models to compare and find equivalent fractions
- Multiplication and division of whole numbers

Pre and Post Assessments

Pre and post assessments in unit.
Exit slips (teacher developed and from unit)

Preassessment for classroom demo – see attached.
(Preassessment based on concepts that will help the teachers know students' current understanding of fractions.)

Other formative assessment opportunities:

- Simultaneous Numbered Heads
- Inquiry Chart
- Work on unit lessons
- Guided math group

Visual Models/ Algorithms/ Diagrams for Compendium

Hand-drawn mathematical diagrams and equations for multiplication and division of fractions:

- $3 \times \frac{3}{4} = \frac{9}{4}$ (with a grid model showing 3 rows of 3/4)
- $\frac{1}{2} \times \frac{1}{4} = \frac{1}{8}$ (with a grid model showing 1/2 of 1/4)
- $3 \div \frac{1}{3} = 9$ (with a number line from 0 to 3 and a stack of 9 blocks)
- $\frac{1}{2} \div 3 = \frac{1}{6}$ (with a grid model showing 1/2 divided into 3 parts)
- Number line from 0 to 1 with tick marks at 0, 1/2, and 1.
- Number line from 0 to 3 with tick marks at 0, 1, 2, and 3.
- Number line from 0 to 1 with tick marks at 0, 1/3, and 1.

Want to include a real-world context with each.

Connections (Real World Applications)

- Dividing food (candy bars, cakes)
- Weight of food ($2\frac{1}{2}$ pounds of grapes X $1\frac{1}{4}$ times that weight in bananas)
- Bags of marbles, boxes of pencils, yards or feet of wrapping paper or ribbon
- Increasing or decreasing recipes, fraction of students on buses
- $\frac{2}{3}$ of the class are boys. $\frac{1}{2}$ are wearing tennis shoes. What fraction of the boys are wearing tennis shoes?

Language Functions/Structures

Describe First we _____. Then we _____. Finally, we _____

Explain We decided to _____ because _____. To divide ___ by ___ you ...
 To solve the problem, we _____ and then _____.
 The product of ___ times ___ is _____ because ...
 The quotient of ___ divided by ___ is _____ because ...
 The answer to ___ divided by ___ is _____ because ...

Basic structures _____ times _____ equals _____. _____ of _____ is _____. What times _____ is _____?
 _____ divided by _____ is _____. How many _____ in _____?

Vocabulary

fraction, numerator, denominator, operations, multiplication/multiply, division/divide, mixed numbers, product, quotient, partition, equal parts, equivalent, factor, unit fraction, benchmark fraction

Focus and Motivation

Chants: Yes Ma'am: Fractions, Decimals, Percents by Annette Maestas
 Fractions Cadence by Evelyn Chávez

Video and quizzes on Brainpop for fractions


Literature: *Inchworm and a Half* by Elinor J. Pinczes
The Wishing Club by Donna Jo Napoli
Engineering Marvels: Roller Coasters: Dividing Fractions by Ben Nussbaum

Activity with pattern blocks or cuisenair rods: If _____ is _____, then what is _____? What would be one whole? What would _____ be?

YouTube - Fractions in real life <https://www.youtube.com/watch?v=5AVjBFP4MRg&t=36s> (possible start for doing a fraction hunt)

Fraction Check-in

Name _____

<p>Solve. Draw a picture or use a number line.</p> <p>$12 \div 4 =$</p>	<p>What happens when you divide a number by another number?</p>
<p>Put these numbers on the number line. $\frac{3}{4}$ $1\frac{1}{2}$ $\frac{1}{3}$ 3 $2\frac{1}{4}$</p> 	
<p>Write or draw what you now about fractions.</p>	<p>Solve. Show your work.</p> <p>$4 \times \frac{1}{2} =$</p>

Yes Ma'am: Fractions, Decimals, Percents
by Annette Maestas

Is this a fraction?	Yes, Ma'am
Is this a fraction?	Yes, Ma'am
How do you know?	Part of a whole
How do you know?	Numerator and denominator
Give me an example.	$\frac{3}{4}$ (3 out of 4)
Give me an example.	$\frac{1}{4}$ (1 out of 4)
Is this a decimal?	Yes, Ma'am
Is this a decimal?	Yes, Ma'am
How do you know?	Part of a whole
How do you know?	Tenths, hundredths, thousandths
Give me an example.	0.16 (sixteen hundredths)
Give me an example.	0.075 (seventy-five thousandths)
Is this a percent?	Yes, Ma'am
Is this a percent?	Yes, Ma'am
How do you know?	Parts of a whole
How do you know?	Compares a number to 100
Give me an example.	25%
Give me an example.	Means 25 out of 100
Are they all alike?	Yes, Ma'am
Are they all different?	Yes, Ma'am
Explain yourself	All parts of a whole
Explain yourself	Represented differently